

Time to finish: 90 min., Resources: pocket calculator, formulary

Date: 08.07.2010

Family Name (legible!): Sem.:

Seat-Nr.:

First Name:

Room-Nr.:

The valid Student ID together with a photo ID have to be presented during the examination!

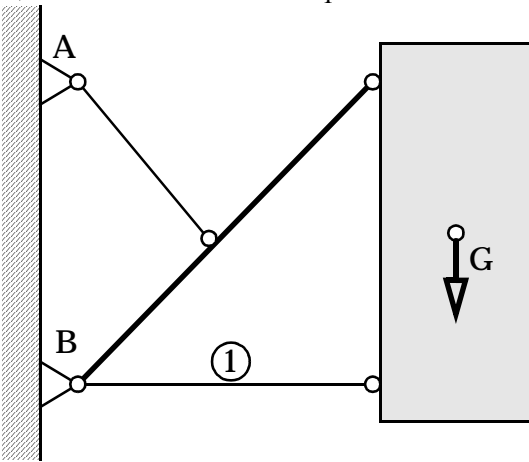
Signature: _____

Supervisor: _____

Task 1: Graphic Solution (12 points)

A body with the dead weight $G=4\text{kN}$ is fixed in the depicted structure.

- a) Determine the support reactions in the bearing A and B graphically!
- b) Determine the force S_1 in strut 1 !



Plan of forces: scale 1cm = 1 kN



Results: $A = 7.8 \text{ kN}$; $B = 5.4 \text{ kN}$; $S_1 = 1.1 \text{ kN}$

Task 2: Rolling resistance (12 points)

A worker moves a wheelbarrow with constant speed.

Given:

Weight of the wheelbarrow

(in centroid S)

$$G = 1000 \text{ N},$$

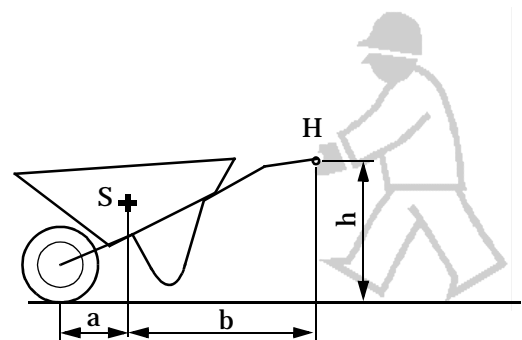
Coefficient of rolling resistance

$$\mu_R = 0.07,$$

Distances: $a = 400 \text{ mm}$; $b = 1000 \text{ mm}$; $h = 830 \text{ mm}$.

To be determined: Resultant of handforce H.

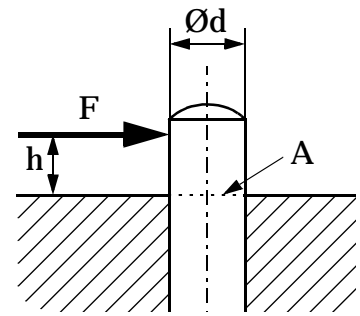
$[H = 260 \text{ N}]$



Task 3: Shear pin (7 points)

A cylindrical steel pin is clamped rigidly and subject to a force F as shown.

Given: $\varnothing d = 10\text{mm}$; $h = 4\text{mm}$; $F = 8\text{kN}$;
flexural yield strength: $s_{bF} = 400\text{N/mm}^2$.



To be determined for the cross section A at the rigid clamping:

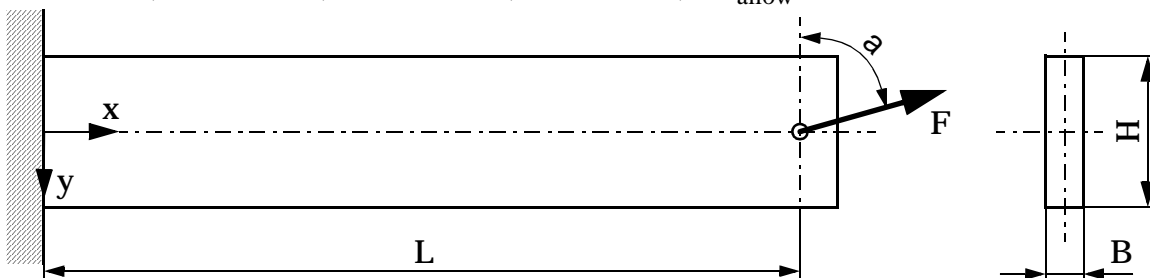
- Safety factor S_{Fb} against plastic flow due to max. bending stress s_b ,
- Safety factor S_{Fq} against plastic flow due to max. shear stress t_q .

$[a) S_{Fb} = 1.23 \quad b) S_{Fq} = 1.70]$

Task 4: Combined normal stress (16 points)

The sketched cantilever is subject to a force F as shown.

Given: $L=1\text{m}$; $B=50\text{mm}$; $H=200\text{mm}$; $\alpha=80.54^\circ$; $s_{\text{allow}} = 100\text{N/mm}^2$.



- Sketch in into the drawing at any position x :
the distribution of the total normal stress over the height of the beam qualitatively.
- Calculate the location x_0 at which compressive stress begins to occur.

$[x_0 = 800\text{mm}]$

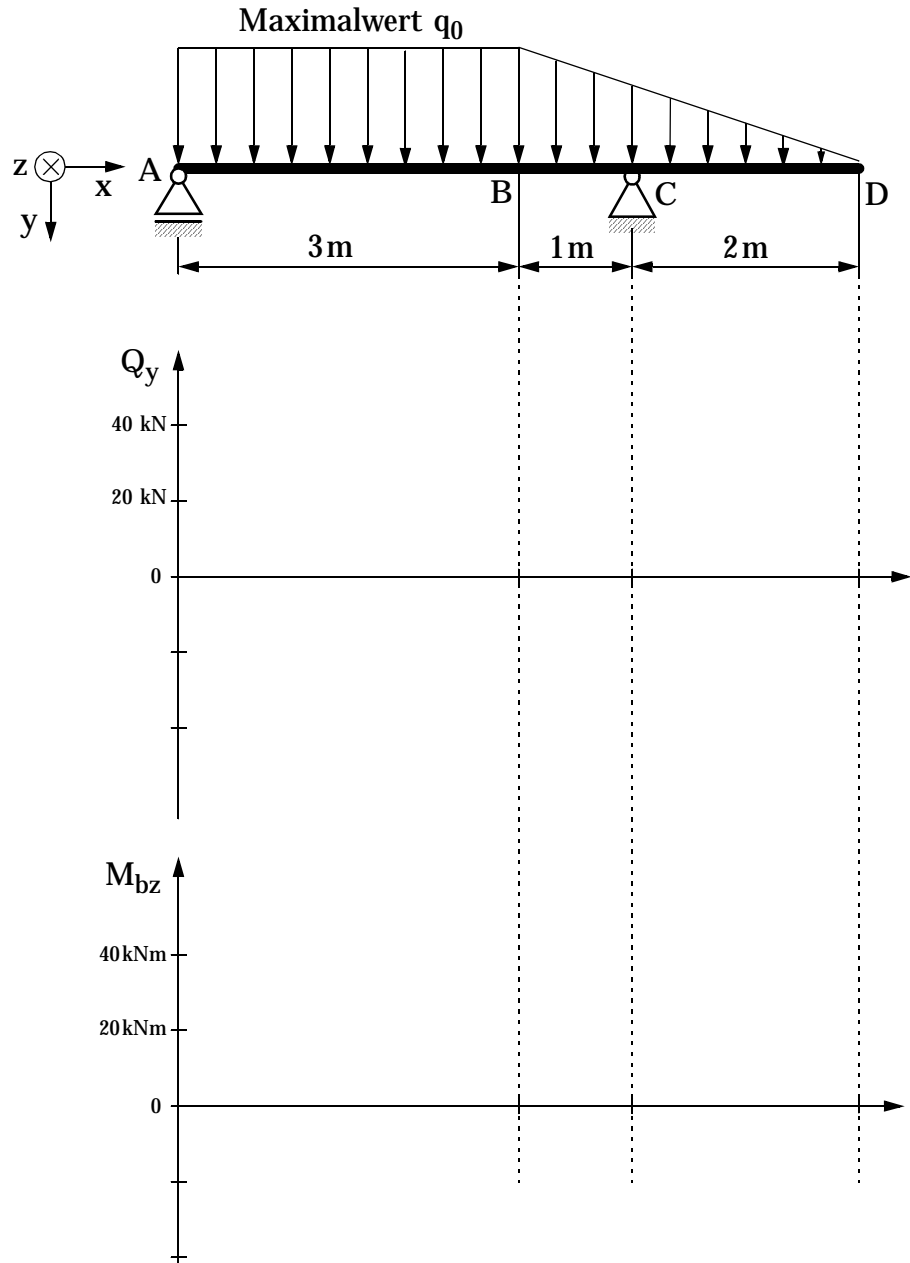
- Calculate the maximum of the force F so that the allowable total normal stress s_{allow} is not exceeded.

$[F = 169\text{kN}]$

Task 5: Stress resultants (25 points)

Given: A girder with both a constant and a linear decreasing line load $q(x)$;
 $q_0 = 24\text{kN/m}$; Distances as shown.

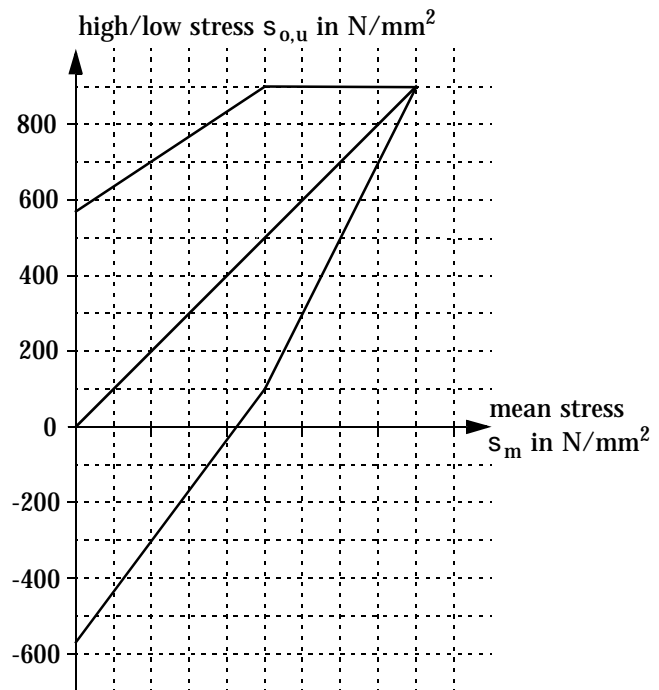
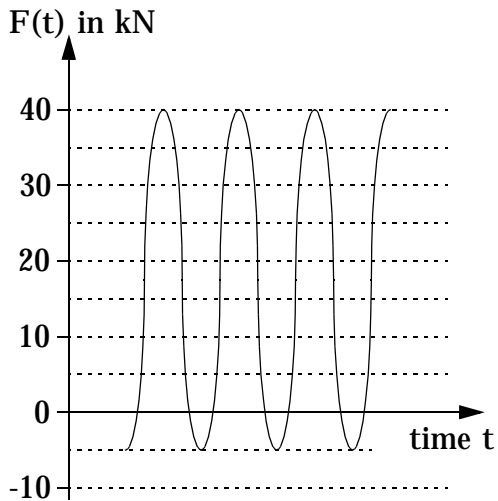
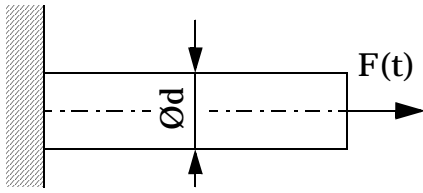
To be determined: a) the support reactions in the bearings A and C,
 b) Profile of both transverse force Q_y and bending moment M_{bz} including the numerical values in B and C
 c) exact position and numerical value of the maximum bending moment M_{bz} .



[a) $A=45\text{kN}$ $C=63\text{kN}$ c) $M_{bz\max}=42.2\text{kNm}$ at $x=1.875\text{m}$]

Task 6: Long life fatigue strength (11 points)

A girder (diameter $d=10.55\text{ mm}$) is subject to a dynamic compressive-/tensile-force $F(t)$ (with constant mean load). Furthermore the Smith-diagram of the used material is given.



a) Calculate the safety factor S_D against endurance failure.

$$[S_D = 1.94]$$

b) Calculate the safety factor S_F against plastic flow.

$$[S_F = 1.97]$$

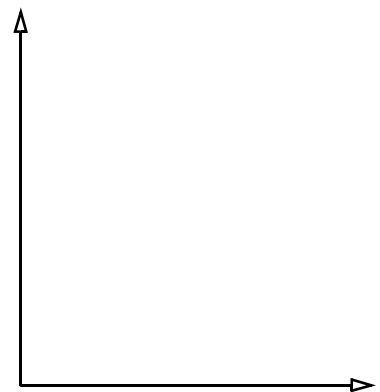
Task 7: Tensile Test (8 points)

A rubber cord (length $l=200\text{ mm}$; quadratic cross section with edge length $a_0=2\text{ mm}$) is stretched by a tensile force linear-elasticly.

a) Plot the curve of this tensile test in a stress-strain diagram (into the depicted coordinate system)! Show how to find Young's modulus with the help of the diagram (sketch it in!)

b) Calculate Young's modulus for this rubber material.

$$[E = 25\text{ N/mm}^2]$$



c) Poisson's ratio for rubber material is $\nu=0.5$. To which value a_1 will the edge length change while carrying out this tensile test.

$$[a_1 = 1.9\text{ mm}]$$