

Time to finish: 60 min

24.07.2020

Allowed resources: pocket calculator, all documents used in hardcopy paperwork

Name: ..... Sem.: ..... Seat-Nr.: .....

First Name: ..... Room-Nr.: .....

Valid student ID together w/ a photo ID to be available during examination

Signature: ..... Invigilator: .....

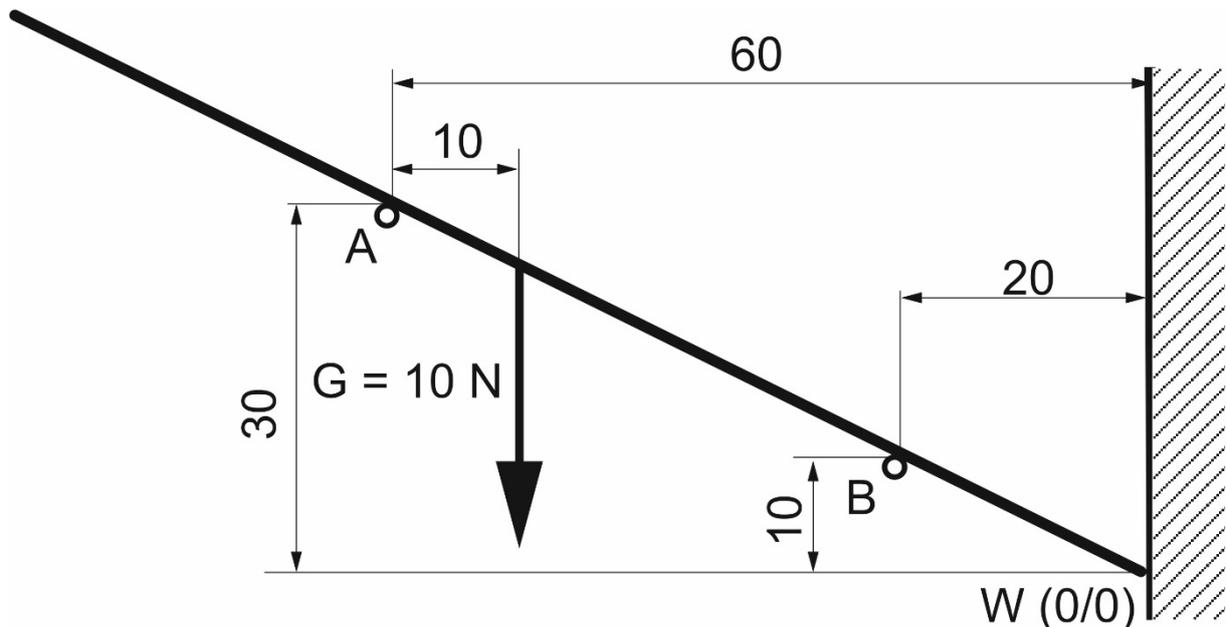
**Task 1: Graphic Solution (12 points)**

The beam is supported on both the two rods and the wall as shown. All supports/contact points are frictionless. The gravitational force  $G$  acts at the sketched position.

Determine the forces at the positions A, B and W graphically.

Transfer the drawing to your sheet of paper for finding the solution. Use the given dimensions therefore.

(scale 1 cm = 2 N)



Solution: A = [5,6] N, B = [5,5] N, W = [5,0] N

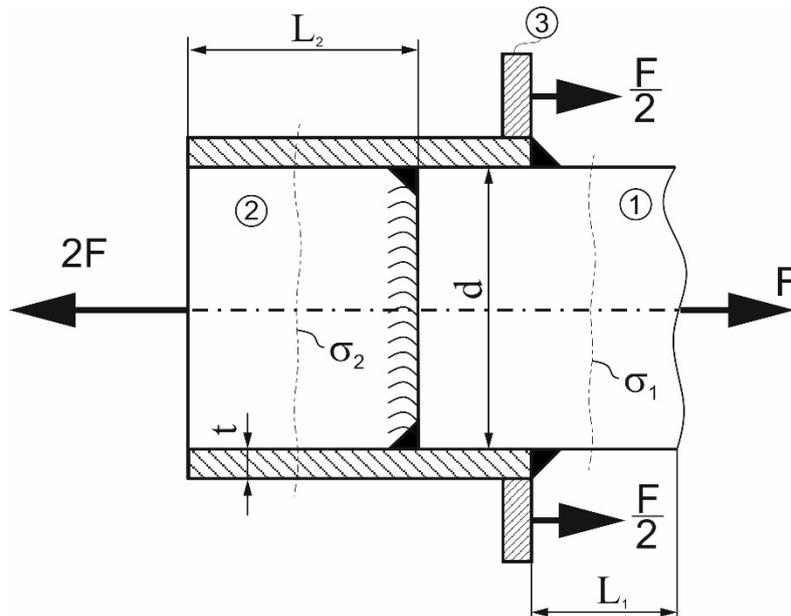
**Task 2: Stresses (15 points)**

The welded design is given as shown. The tube ② is subjected to the force  $2F$  on the left side, while both the flange ③ and the rod ① are each subjected to the forces  $F$ .

Given:  $F = 15 \text{ kN}$        $L_1 = 50 \text{ mm}$        $d = 50 \text{ mm}$        $t = 5 \text{ mm}$

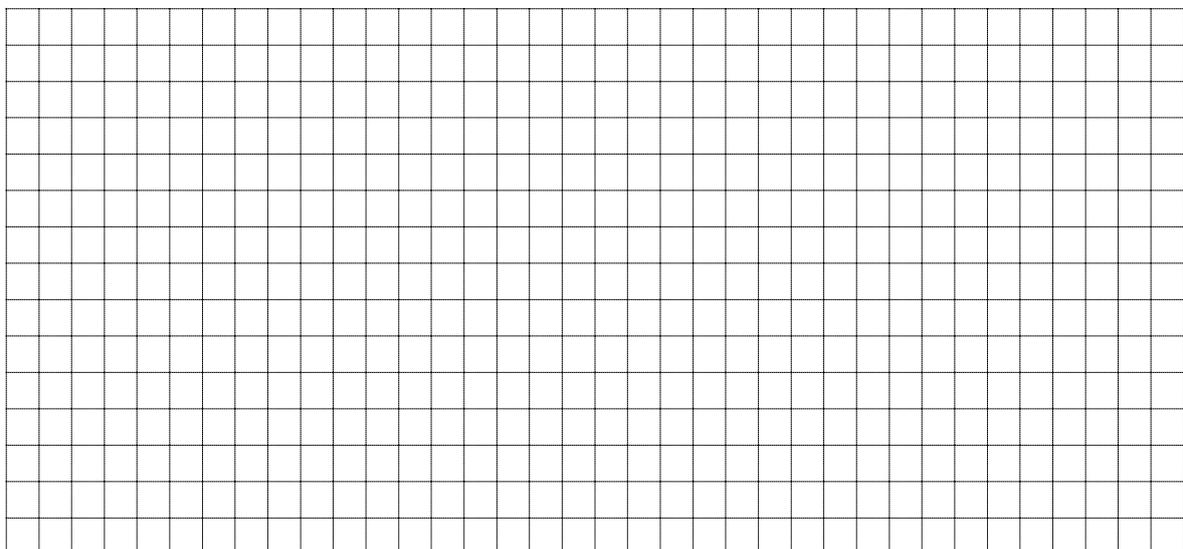
Young's modulus tube  $E_2 = 110000 \text{ N/mm}^2$

Young's modulus rod  $E_1 = 70000 \text{ N/mm}^2$       Poisson's ratio rod  $\nu = 0,3$

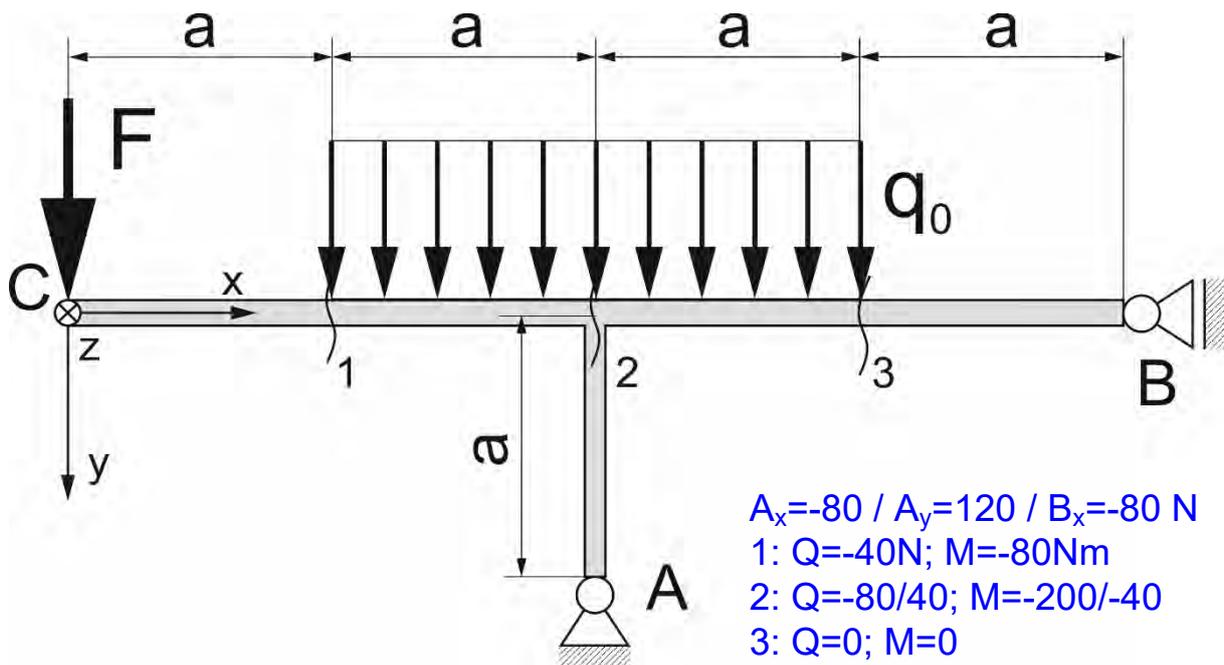


- Determine the normal stress  $\sigma_1$  in the rod ① within the marked section.
- Determine the normal stress  $\sigma_2$  in the tube ② within the marked section.
- Determine the change in length  $\Delta L_1$  within the marked section  $L_1$ .
- Determine  $L_2$  such, that the change in length of the tube is equal to  $\Delta L_1$ .
- Determine the change in diameter within the rod ①.

- 7,6 N/mm<sup>2</sup>
- 34,7 N/mm<sup>2</sup>
- 5,5  $\mu\text{m}$
- 17,4 mm
- 1,6  $\mu\text{m}$



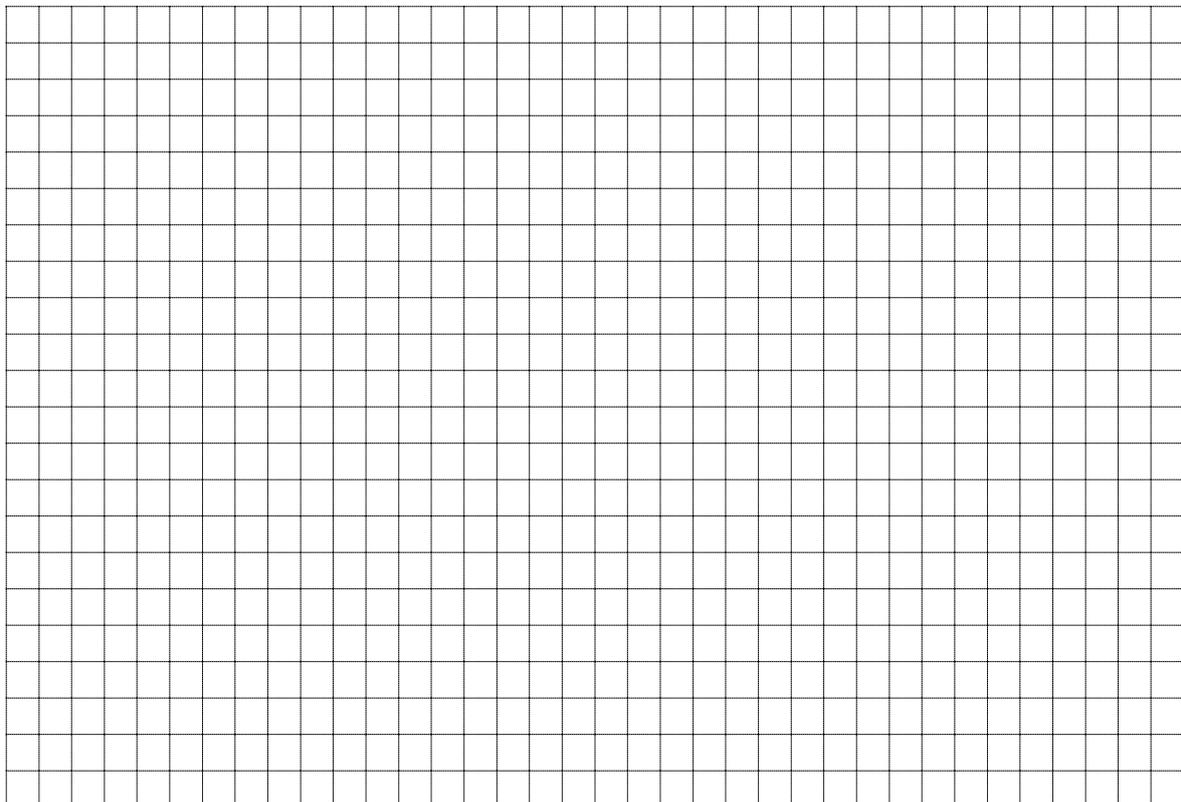
**Task 3: Stress resultants (20 points)**



A beam is mounted in point B and, via support, in point A. The load  $F$  acts in point C against the beam. Additionally the line load  $q_0$  acts in the middle of the beam.

Given:  $F = 40 \text{ N}$        $q_0 = 20 \text{ N/m}$        $a = 2 \text{ m}$

- a) Determine the support reaction forces  $A_x$ ,  $A_y$  and  $B_x$ .
- b) Determine the run of both the transverse force and the bending moment within the beam all the way from C to B, incl. the numerical values at the positions 1, 2 and 3.

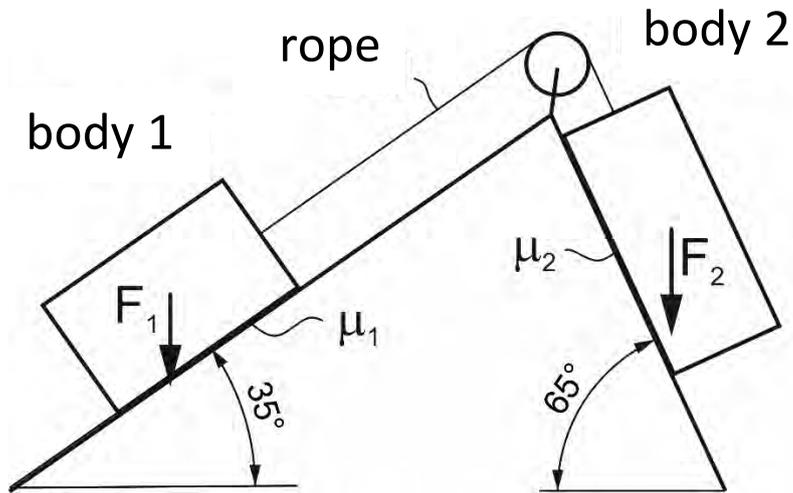


**Task 4: Friction (13 points)**

Both bodies are loaded by the gravitational forces  $F_1$  respectively  $F_2$  and they are connected with each other by a rope as shown. The pulley is frictionless.

Determine the coefficient of friction  $\mu_2$  between body 2 and the ramp such, that it can slide down with constant velocity. How large is the rope force  $S$  in that case?

Given:  $F_1 = F_2 = 100 \text{ N}$ ,  $\mu_1 = 0,2$



$\mu_2 =$  [0,4]

$S =$  [73,8 N]

